

17EC42 **USN** 

## Fourth Semester B.E. Degree Examination, Aug./Sept.2020 Signals and Systems

Time: 3 hrs. Max. Marks: 100

Note: 1. Answer any FIVE full questions, choosing ONE full question from each module. 2. Missing data, if any, may be suitably assumed.

## Module-1

- 1 Explain the following with an example each:
  - i) Even and odd signal
  - ii) Aperiodic and periodic signal
  - iii) Energy and power signal.

(06 Marks)

- b. Sketch the following signal:
  - i) y(t) = r(t+2) r(t+1) r(t-1) + r(t-2)
  - ii) y(t) = r(t+2) r(t+1) r(t-1) + r(t-2)

(06 Marks)

c. Verify the following properties of system:

memoryless, casual, stable and some invariant y(n) = n x(n).

(08 Marks)

Sketch the even and odd parts of the signal shown in the Fig.Q2(a)

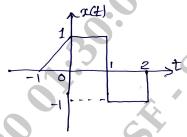


Fig.Q2(a) (06 Marks)

- b. Classify the following the following as an energy or power signal
  - i) y(t) = r(t) r(t-2)

ii) 
$$x(t) = (1 + e^{-5t})u(t)$$
.

(08 Marks)

- Determine whether the following signals are periodic or not. If periodic find its fundamental time period.

ii) 
$$x(t) = \cos t + \sin \sqrt{2}t$$
.

(06 Marks)

## Module-2

- Prove the following properties of convolution: 3
  - i) Commutative ii) Distributive.

(06 Marks)

Determine the convolution of the following two signals  $x(t) = e^{-3t}u(t)$  and h(t) = u(t+2).

(07 Marks)

Find the convolution of the following sequences

$$x(n) = \beta^{n}u(n)$$
 with  $|\beta| < 1$  and  $h(n) = u(n-3)$ .

(07 Marks)

OR

- 4 a. Determine the convolution sum of the given sequence  $x(n) = \{1, 2, 3, 1\}$  and  $h(n) = \{1, 2, 1, -1\}$  sketch output. (06 Marks)
  - b. The impulse response of the system is given by h(t) = u(t). Determine the output of the system for an input  $x(t) = e^{-\alpha t} u(t)$ . (08 Marks)
  - c. Prove the associative property of convolution.

(06 Marks)

Module-3

- 5 a. Find the step response for the impulse response h(t) = u(t+1) u(t-1). (06 Marks) b. Find the overall impulse response of a cascade of two systems having identical impulse
  - b. Find the overall impulse response of a cascade of two systems having identical impulse responses h(t) = 2[u(t) u(t-1)]. (06 Marks)
  - c. Find the Fourier series coefficients X(k) for the signal  $x(t) = \sum_{m=-\infty}^{\infty} [\delta(t \frac{1}{2}m)]$ . Sketch the magnitude and phase spectra. (08 Marks)

OR

- 6 a. Determine whether following system with the given impulse response is memoryless, causal and stable  $h[n] = \left[\frac{1}{2}\right]^n u[n]$ . (06 Marks)
  - b. Evaluate the DTFS representation for the signal x(n) shown in Fig.6(b) and sketch its spectra.

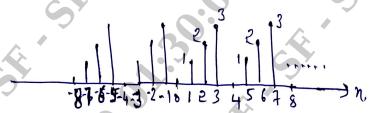


Fig.Q6(b) (08 Marks)

c. Find the Fourier series representation for the signal  $x(t) = \sin(2\pi t) + \cos(3\pi t)$ . Sketch the magnitude and phase spectra. (06 Marks)

**Module-4** 

- 7 a. Prove the following properties of Fourier transform:
  - i) Time shifting
  - ii) Time domain convolution.

(08 Marks)

b. Find the Fourier transform of the signal.

(06 Marks)

c. Find the DTFT of the signal shown in the Fig.Q7(c).

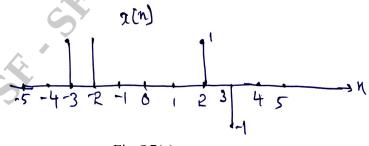


Fig.Q7(c)

(06 Marks)

OR

- 8 a. Explain the concept of sampling theorem and reconstruction of signals. (06 Marks)
  - b. Find the DTFT of the sequence  $x(n) = -a^n u[-n-1]$ . (08 Marks)
  - c. Find the Fourier transform of the signal  $x(t) = e^{-3t} u(t-1)$ . (06 Marks)

Module-5

- 9 a. Explain the properties of ROC. (05 Marks)
  - b. Find the Z-transform and the ROC of the discrete sinusoid signal.  $x[n] = [\sin(\Omega n)]u[n]$ . (07 Marks)
  - c. Find the transfer function and difference equation if the impulse response is

$$h[n] = \left[\frac{1}{3}\right]^n u[n] + \left[\frac{1}{2}\right]^n u[n-1].$$
 (08 Marks)

OR

- 10 a. Using power series expansion technique or long division method find the inverse z-transform of the following X(z).
  - i)  $X(z) = \frac{z}{2z^2 3z + 1}$ ; ROC  $|z| < \frac{1}{2}$

ii) 
$$X(z) = \frac{z}{2z^2 - 3z + 1}$$
; ROC  $|z| > 1$ . (08 Marks)

- b. Determine the z-transform of the following signal  $x[n] = 2^n u[n]$ .
  - Also obtain ROC and locations of poles and zeroes of X(z). (06 Marks)
- c. Using z-transform find the convolution of the following two sequences

$$\begin{split} h[n] &= \left\{\begin{matrix} 1, & \frac{1}{2}, & \frac{1}{4} \end{matrix}\right\} and \\ x[n] &= \delta\left[n\right] + \delta\left[n-1\right] + 4\delta\left(n-2\right). \end{split} \tag{06 Marks)} \end{split}$$

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